

COMPLEX DYNAMIC PHENOMENA IN
ENVIRONMENTAL PLANNING AND MANAGEMENT
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1. ENVIRONMENTAL MANAGEMENT AND NONLINEAR DYNAMICS

An overview of the most typical problems one encounters in environmental planning and management. Emphasis on relationships with nonlinear dynamics. Further reading: *Journal of Environmental Management* (1996), 48, 357-373.

2. THE PROBLEM OF FLOATING PLANTS IN RESERVOIRS

Description of the problem through a model of competition between floating and submerged plants. Analysis of the model: alternative stable states. Bifurcation analysis and derivation of possible control actions. Analysis of the history of Lake Kariba on the Zambesi river. Further reading: *PNAS* (2003), 100, 4040-4045.

3. FOREST EXPLOITATION AND ACID RAIN: A DANGEROUS MIX

Description of the problem through a series of minimal models. Existence of catastrophic bifurcations (forest collapse). Cusp bifurcation: negative synergistic effect of acid rain and exploitation.

Further reading: *Vegetatio* (1987), 69, 213-222

Appl. Math. Modelling (1989), 13, 674-681

Theor. Pop. Biol. (1998), 54, 257-269.

4. THE RECLAMATION OF EUTROPHIC WATER BODIES

Description of the problem in terms of minimal models involving algae, zooplankton and planktivorous fish. Analysis of the bifurcations of the model: the appearance and disappearance of clear-water regimes. Biological control. Further reading: *OIKOS* (1997), 80, 519-532.

5. TOURISM SUSTAINABILITY: AN OVERVIEW

The three components of the problem: tourists, environment and facilities. Detection of possible scenarios. Profitable, compatible and sustainable policies. Adaptivity. The case of alternative classes of tourists and of diversified investments.

Further reading: *Conservation Ecology* (2002), 6(1): 13 [online].

Chaos and Complexity Letters (2004) first issue (in the press).

6. ENRICHMENT AND YIELD MAXIMIZATION

Exploitation of renewable resources. Enrichment and mean yield maximization. Analysis of the case of tritrophic food chains. Optimality at the edge of chaos. Derivation of management rules.

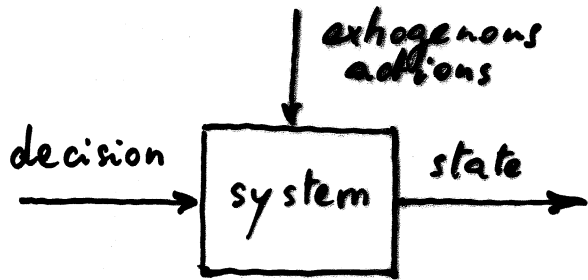
Further reading: *Am. Nat.* (1997) 150, 328-345

Bull. Math. Biol. (1998) 60, 703-719

Ecol. Lett. (1999) 2, 6-10

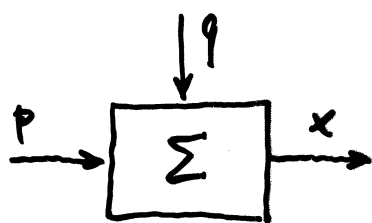
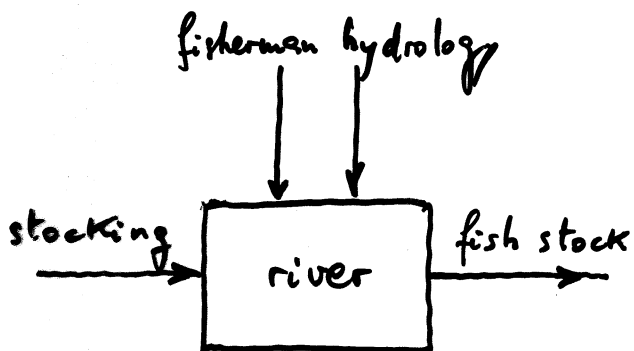
J. Math. Biol. (2002) 45, 396-418.

PLANNING



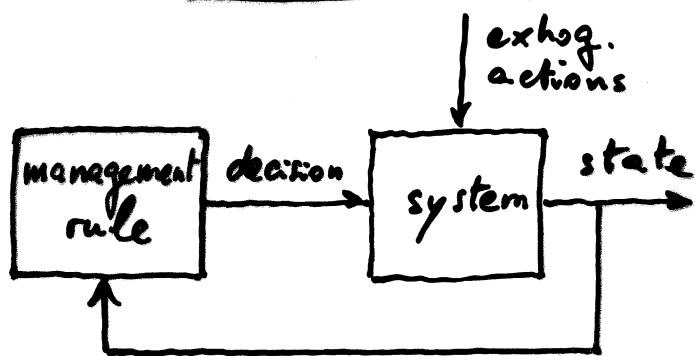
select the best decision
and keep it fixed forever

open loop control



$$\dot{x}(t) = f(x(t), p, q)$$

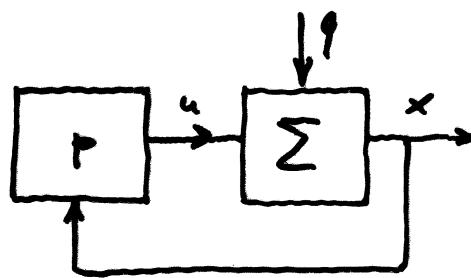
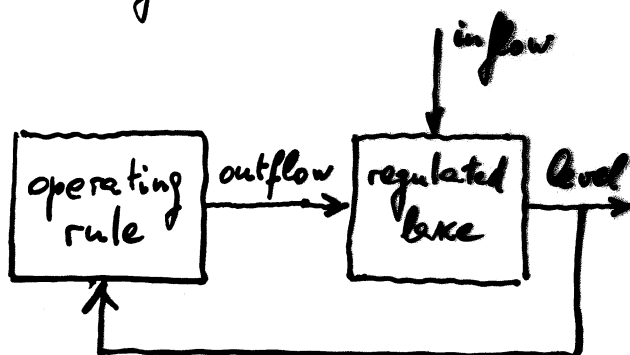
MANAGEMENT



select the best management
rule and use it forever

closed loop control

↑
feedback



$$\dot{x}(t) = \underbrace{g(x(t), u(p, x(t), q))}_{f(x(t), p, q)}$$

About the system

continuous-time finite dimension
 discrete-time " "
 finite (automaton) "
 infinite-dimensional
 probabilistic automaton
 CNN
 :

About disturbances

constant known/unknown
 periodic $q \sin(\omega t)$
 stochastic process
 :

Constraints

on p
 on q
 on x
 budget constraints

Available information

on Σ
 on q (known, measurable,
 predictable, ...)
 adaptive control

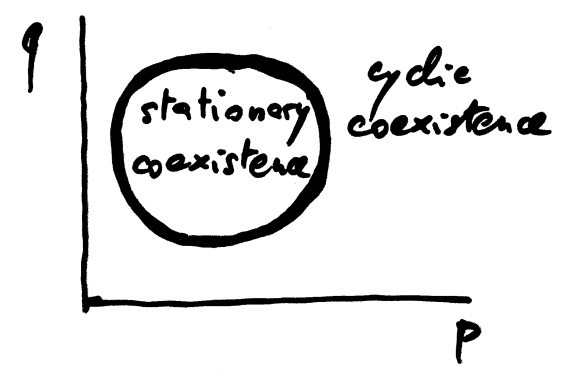
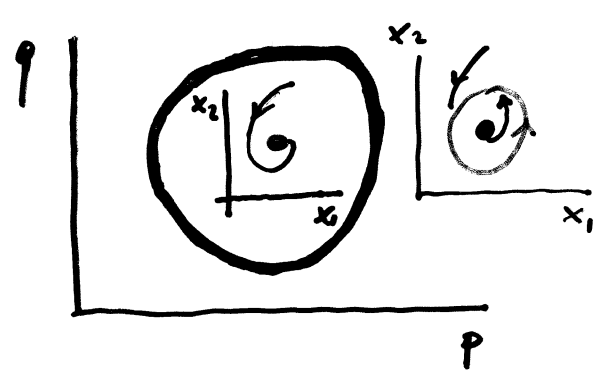
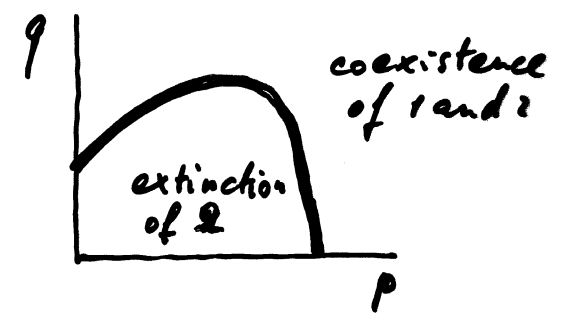
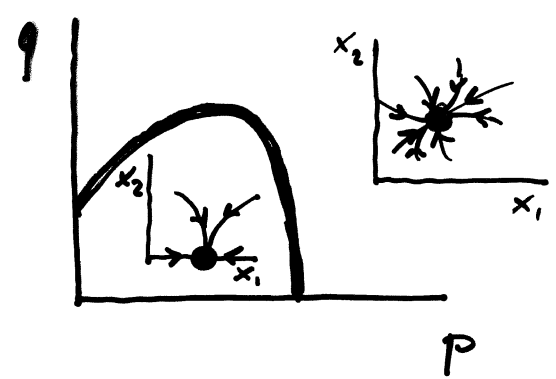
Choice of p

from experience
 optimality arguments
 (expectation, min variance,
 min max, ...)

$$\dot{x} = f(x, p, q)$$

PROBLEM : what happens if p and/or q are changed ?

Small variations of p and or q can generate qualitatively important changes of the behavior of the system

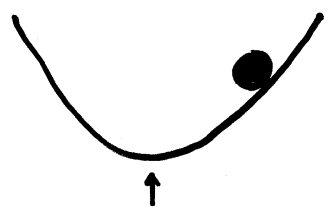


On opposite sides of the curve the asymptotic behavior of the system is qualitatively different

These curves are called bifurcation curves.

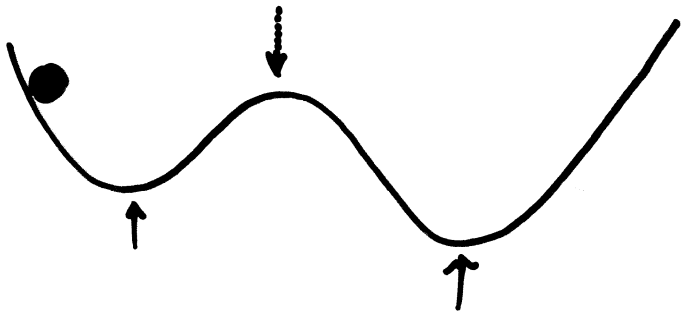
MULTIPLE ATTRACTORS AND CATASTROPHES

In the two previous examples the asymptotic behavior of the system does not depend upon initial conditions

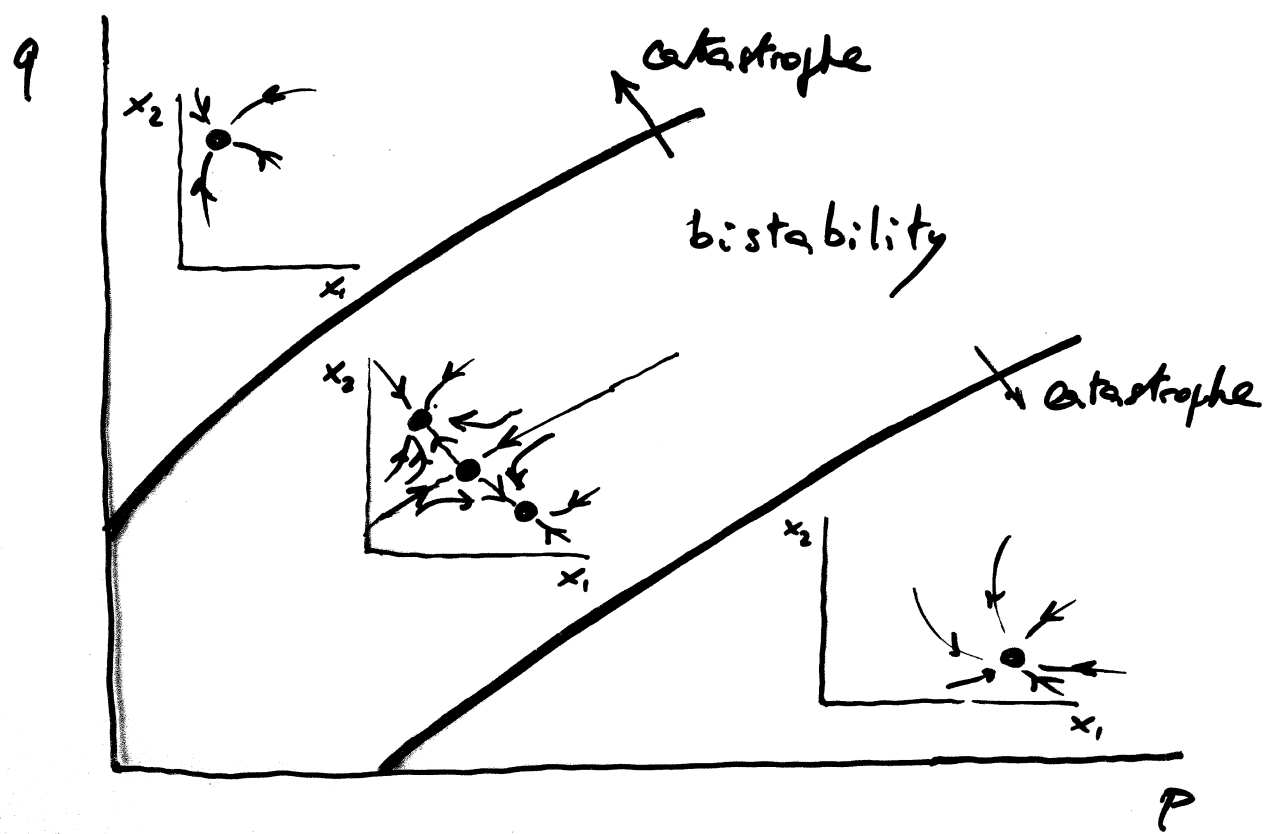


unique stable equilibrium

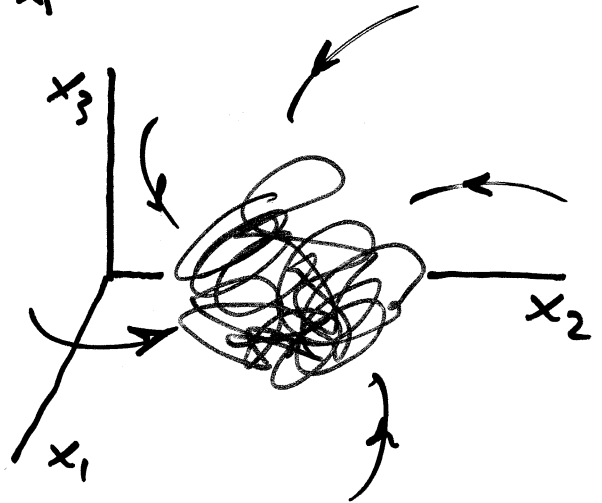
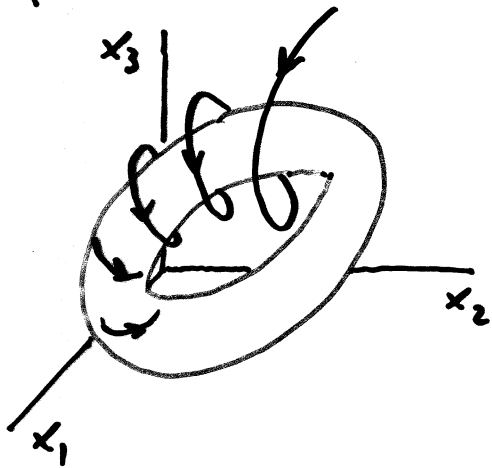
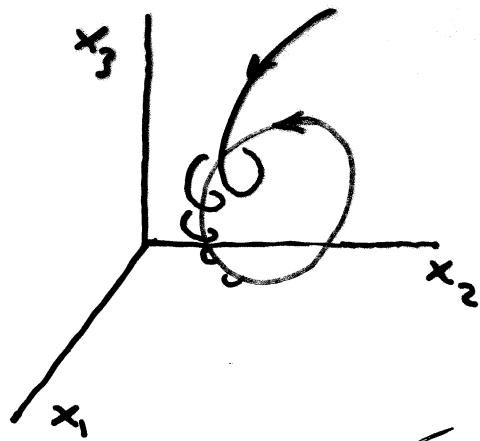
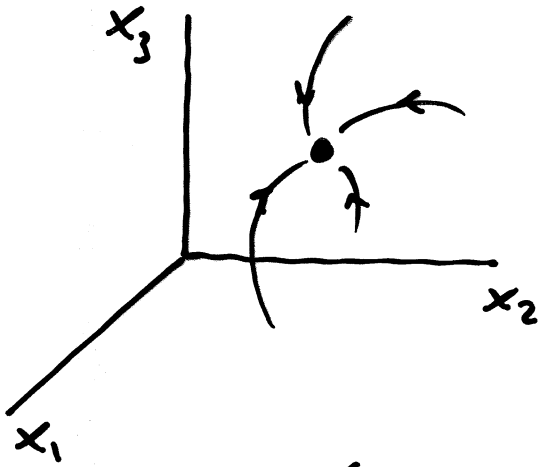
In other cases the asymptotic behavior of the system depends upon initial conditions



2 stable equilibria
1 unstable equilibrium

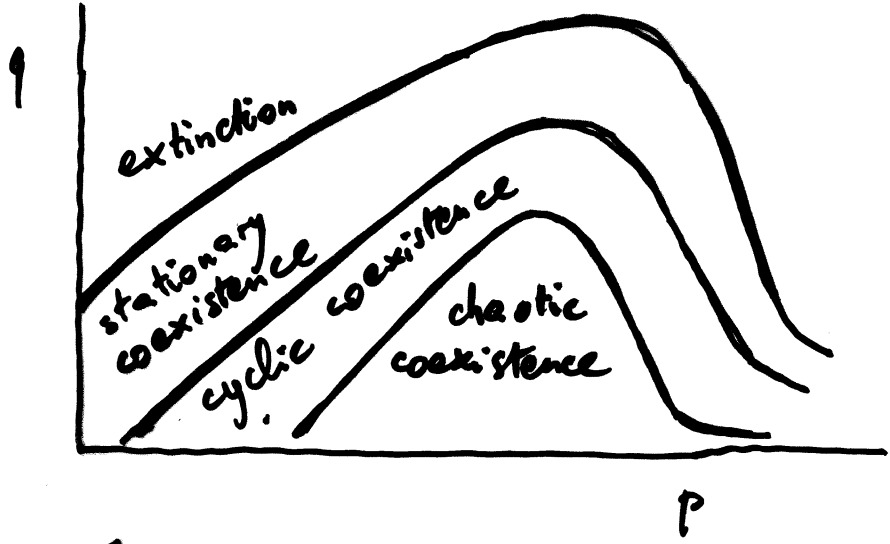


SIMPLE AND COMPLEX ATTRACTORS



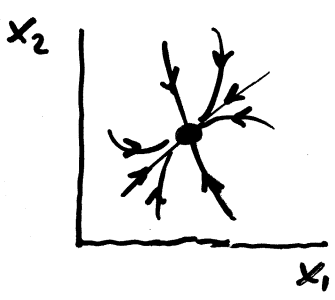
- equilibrium → stationary regime
- cycle → cyclic (periodic) regime
- torus → quasiperiodic regime
- strange attractor → chaotic regime

CHANGE OF REGIME

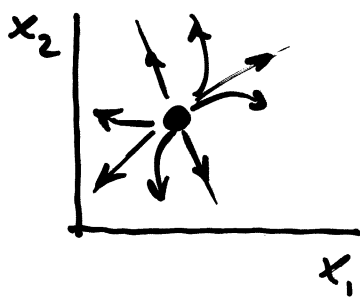


In this figure each bifurcation curve corresponds to a change of regime

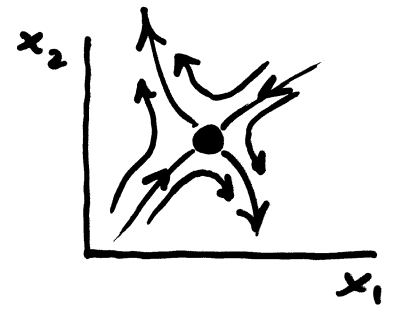
ATTRACTORS , REPELLORS AND SADDLES



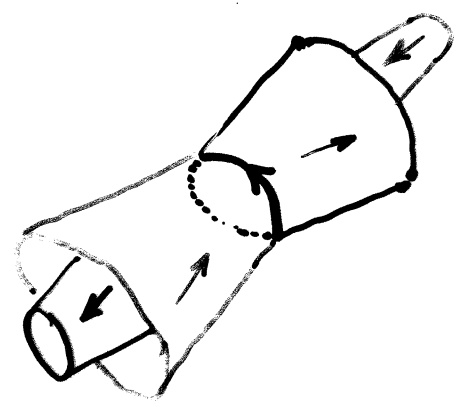
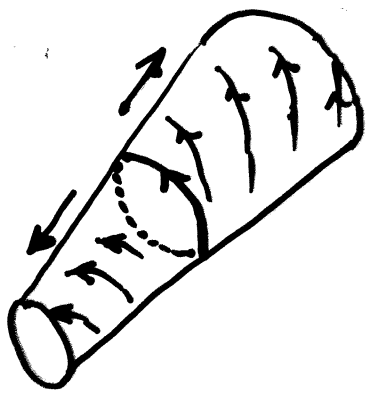
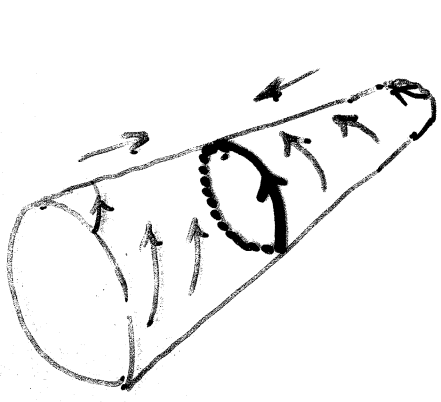
attractor

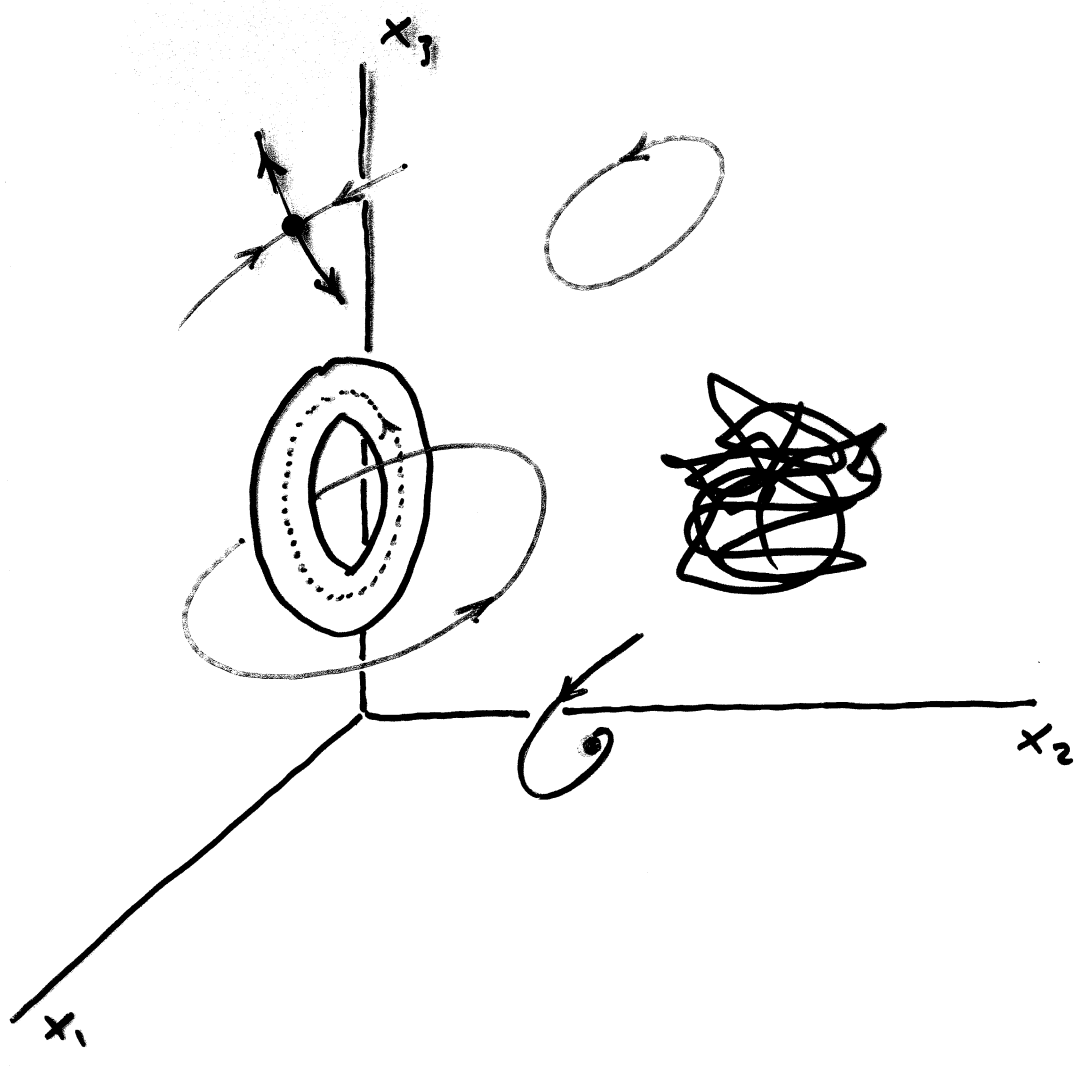


repellor



saddle





If attractors, repellors and saddles are separated for a given value (p, q) of parameters, they remain separated for a small perturbation of the parameters.

In other words, small parameter perturbations cannot give rise to qualitatively significant changes.

Thus : bifurcations correspond to collisions of attractors, repellors and saddles

Example (Pollution control : see further reading)

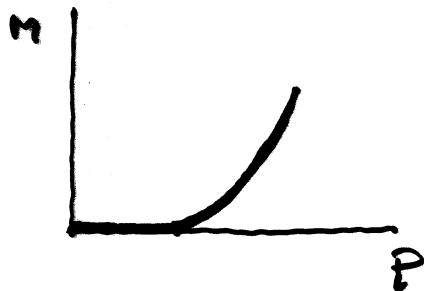
R = resource
 P = pollution
 C = capital

$$\dot{R} = R(1-R) - M(P)R + s$$

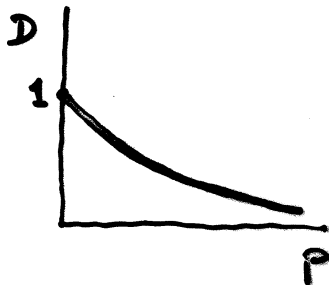
$$\dot{P} = w D(C) - a P - b P R$$

$$\dot{C} = -e C + \underbrace{f \cdot D(C) \cdot \pi(R, P)}_{\text{investment}}$$

↑ perception function



excess mortality



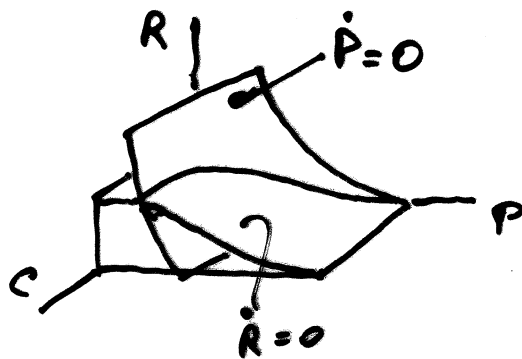
pass-through function

Case 1 $\dot{C} = 0 \Leftrightarrow C = \text{const.} \Leftrightarrow$ maintain C constant

Case 2 $\dot{C} \neq 0 \quad \pi = \pi(R)$

Case 3 $\dot{C} \neq 0 \quad \pi = \pi(P)$

CASE 1



CASE 2

CASE 3

see paper